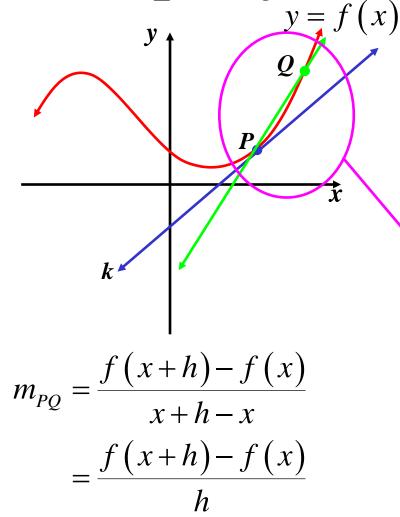
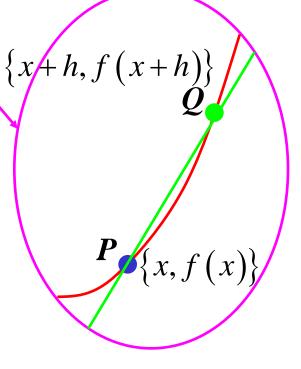
The Slope of a Tangent to a Curve



To find the exact value of the slope of k, we calculate the limit of the slope PQ as h gets closer to 0.

Slope PQ is an estimate for the slope of line k.

- A: As close to **P** as possible.



slope of tangent =
$$\lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$$

This is known as the "derivative of y with respect to x" and is symbolised; $\frac{dy}{dx}$, y', f'(x), $\frac{d}{dx}\{f(x)\}$ the derivative of y with respect to x" and is

$$f'(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$$

the derivative measures the rate of something changing

The process is called "differentiating from first principles" e.g. (i) Differentiate y = 6x + 1 by using first principles.

$$f(x) = 6x + 1$$

$$f(x+h) = 6(x+h) + 1$$

$$= 6x + 6h + 1$$

$$\frac{dy}{dx} = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$$

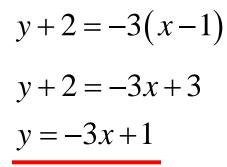
$$= \lim_{h \to 0} \frac{6x + 6h + 1 - (6x+1)}{h}$$

$$= \lim_{h \to 0} \frac{6h}{h}$$

$$= \lim_{h \to 0} 6$$

$$= 6$$

Find the equation of the tangent to $y = x^2 - 5x + 2$ at the point (1, -2). (ii) $f(x) = x^2 - 5x + 2$ $f(x+h) = (x+h)^2 - 5(x+h) + 2$ $= x^{2} + 2xh + h^{2} - 5x - 5h + 2$ $\frac{dy}{dx} = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$ $=\lim \frac{x^2 + 2xh + h^2 - 5x - 5h + 2 - x^2 + 5x - 2}{2}$ $h \rightarrow 0$ $=\lim_{h\to 0}\frac{2xh+h^2-5h}{h}$ $= \lim 2x + h - 5$ $h \rightarrow 0$ =2x-5when x = 1, $\frac{dy}{dx} = 2(1) - 5$ = -3 \therefore the slope of the tangent at (1, -2) is -3



Exercise 7B; 1, 2adgi, 3(not *iv*), 4, 7ab *i*,*v*, 12 (just h approaches 0)