

Calculus Rules

2. Product Rule $\frac{d}{dx}(uv) = uv' + vu'$

“Write down the FIRST and DIFF the SECOND, **PLUS** write down the SECOND and DIFF the FIRST”

e.g. (i) $y = x^7(x^9 - 6)$

$$\begin{aligned}\frac{dy}{dx} &= (x^7)(9x^8) + (x^9 - 6)(7x^6) \\ &= 9x^{15} + 7x^{15} - 42x^6 \\ &= \underline{16x^{15} - 42x^6}\end{aligned}$$

(ii) $y = (x - 2)(2x - 3)$

$$\begin{aligned}\frac{dy}{dx} &= (x - 2)(2) + (2x - 3)(1) \\ &= 2x - 4 + 2x - 3 \\ &= \underline{4x - 7}\end{aligned}$$

(iii) $\frac{d}{dx}\{(x^7 - x^3)(3x^2 + 7)\}$

$$\begin{aligned}&= (x^7 - x^3)(6x) + (3x^2 + 7)(7x^6 - 3x^2) \\ &= 6x^8 - 6x^4 + 21x^8 - 9x^4 + 49x^6 - 21x^2 \\ &= \underline{27x^8 + 49x^6 - 15x^4 - 21x^2}\end{aligned}$$

$$(iv) \ y = 3x(x^2 + 4)^5$$

$$\frac{dy}{dx} = (3x) \left\{ 5(x^2 + 4)^4 (2x) \right\} + (x^2 + 4)^5 (3)$$

$$= 30x^2 (x^2 + 4)^4 + 3(x^2 + 4)^5$$

$$= (x^2 + 4)^4 \left\{ 30x^2 + 3(x^2 + 4) \right\}$$

$$= (x^2 + 4)^4 (33x^2 + 12)$$

$$= \underline{3(x^2 + 4)^4 (11x^2 + 4)}$$

$$(v) \ y = 2x\sqrt{2x-1}$$

$$= 2x(2x-1)^{\frac{1}{2}}$$

$$\frac{dy}{dx} = (2x) \left\{ \frac{1}{2}(2x-1)^{-\frac{1}{2}} (2) \right\} + (2x-1)^{\frac{1}{2}} (2)$$

$$= (2x)(2x-1)^{-\frac{1}{2}} + 2(2x-1)^{\frac{1}{2}}$$

$$= 2(2x-1)^{-\frac{1}{2}} \left\{ x + (2x-1) \right\}$$

$$= 2(2x-1)^{-\frac{1}{2}} (3x-1)$$

**Exercise 7F; 1ac, 2bdf,
3a, 4ad, 5, 6ac,
7, 9, 13a***

$$\underline{\underline{\frac{dy}{dx} = \frac{2(3x-1)}{\sqrt{2x-1}}}}$$