

Calculus Rules

3. Quotient Rule

$$\frac{d}{dx} \left(\frac{u}{v} \right) = \frac{vu' - uv'}{v^2}$$

“SQUARE the BOTTOM, write down the BOTTOM and DIFF the TOP, **MINUS** write down the TOP and DIFF the BOTTOM”

$$\text{e.g. } (i) \quad y = \frac{x}{1+2x}$$

$$\frac{dy}{dx} = \frac{(1+2x)(1) - (x)(2)}{(1+2x)^2}$$

$$= \frac{1+2x-2x}{(1+2x)^2}$$

$$= \frac{1}{(1+2x)^2}$$

$$(ii) \quad y = \frac{2x}{\sqrt{x^2-4}}$$

$$\frac{dy}{dx} = \frac{(x^2-4)^{\frac{1}{2}}(2) - (2x)\left\{ \frac{1}{2}(x^2-4)^{-\frac{1}{2}}(2x) \right\}}{(x^2-4)}$$

$$= \frac{2(x^2-4)^{\frac{1}{2}} - 2x^2(x^2-4)^{-\frac{1}{2}}}{(x^2-4)}$$

$$= \frac{2(x^2-4)^{-\frac{1}{2}} \{(x^2-4) - x^2\}}{-8(x^2-4)}$$

$$= \frac{-8}{(x^2-4)\sqrt{x^2-4}}$$

4. Reciprocal Rule

$$\frac{d}{dx} \left(\frac{k}{v} \right) = \frac{-kv'}{v^2}$$

“MINUS the DERIVATIVE on the FUNCTION SQUARED”

e.g. (i) $y = \frac{1}{x^2}$

$$\begin{aligned}\frac{dy}{dx} &= \frac{-2x}{x^4} \\ &= \frac{-2}{x^3}\end{aligned}$$

(ii) $y = \frac{6}{4x^2 + 3}$

$$\begin{aligned}\frac{dy}{dx} &= \frac{-6(8x)}{(4x^2 + 3)^2} \\ &= \frac{-48x}{(4x^2 + 3)^2}\end{aligned}$$

Exercise 7G; 1aceg, 2, 4a, 6a, 8a