

# *Indefinite Integral*

$$(1) \int x^n dx = \frac{x^{n+1}}{n+1} + c$$

$$(2) \int (ax+b)^n dx = \frac{(ax+b)^{n+1}}{a(n+1)} + c \quad (\text{must be a linear function})$$

$$\begin{aligned} \text{e.g. (i)} \int (2-5x)^3 dx &= \frac{1}{4(-5)} (2-5x)^4 + c \\ &= -\frac{1}{20} (2-5x)^4 + c \end{aligned}$$

---

$$\begin{aligned}(ii) \int \frac{dx}{(3x+1)^2} &= \int (3x+1)^{-2} dx \\ &= -\frac{1}{3}(3x+1)^{-1} + c \\ &= \frac{-1}{3(3x+1)} + c\end{aligned}$$

---

$$\begin{aligned}(iii) \int \sqrt{2x+1} dx &= \int (2x+1)^{\frac{1}{2}} dx \\ &= \frac{2}{3(2)}(2x+1)^{\frac{3}{2}} + c \\ &= \frac{1}{3}(2x+1)^{\frac{3}{2}} + c \\ &= \frac{1}{3}(2x+1)\sqrt{2x+1} + c\end{aligned}$$

---

**Exercise 11D; 1bei, 2bcg,  
4afh, 5cfi, 6ceh, 7bfil, 8\***