

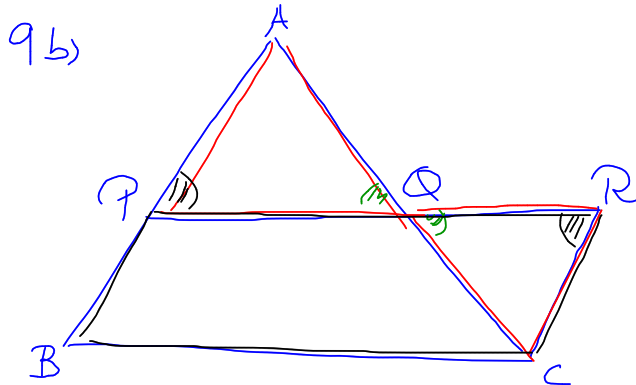
$$A_{\triangle AQR} : A_{\triangle ABC}$$

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$$1 : 4$$

$$\therefore A_{\triangle AQR} : A_{\triangle ABC}$$

$$2 : 4 = 1 : 2$$



$$\frac{PQ}{BC} = \frac{k}{k+l}$$

$$\frac{AP}{BP} = \frac{AQ}{QC} = \frac{k}{l} = \frac{PQ}{QR}$$

$\angle AQP = \angle RQC$  (vertically opposite  $\angle$ 's)

$$\frac{AQ}{QC} = \frac{PQ}{QR} = \frac{k}{l} \text{ (given)}$$

$\therefore \triangle AQP \parallel \triangle CQR$  (SAS, ratio  $k:l$ )

$$\frac{AP}{PB} = \frac{k}{l} \text{ (given)}$$

$$\frac{AP}{RC} = \frac{k}{l} \text{ (ratio sides in } \parallel \text{ } \Delta \text{'s)}$$

$$\therefore PB = RC$$

$\angle APR = \angle QRC$  (matching  $\angle$ 's in  $\parallel \Delta$ 's)

$AB \parallel RC$  (alternate  $\angle$ 's =)

$PRCB$  is  $\parallel$  gram (pair sides = and  $\parallel$ )

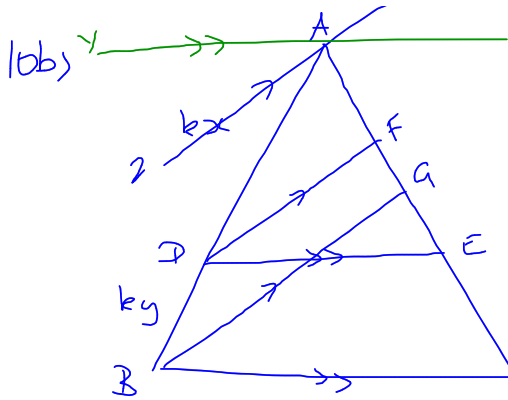
$$\frac{PQ}{BC} = \frac{PQ}{PR}$$

(BC = PR, opposite sides  $\parallel$   $\Rightarrow$  )

$$\frac{PQ}{QR} = \frac{k}{l}$$

$$\begin{aligned} \frac{PQ}{BC} &= \frac{PQ}{PQ + QR} \\ &= \frac{k}{k+l} \end{aligned}$$

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let  $AD:DB$  be  $x:y$   
 construct  $ZA \parallel DF \parallel BC$

$$\frac{AF}{AG} = \frac{AD}{AB}$$

$$= \frac{x}{x+y}$$

construct  $YA \parallel DE \parallel BC$

$$\frac{AD}{AB} = \frac{AE}{AC}$$

$$\frac{x}{x+y} =$$

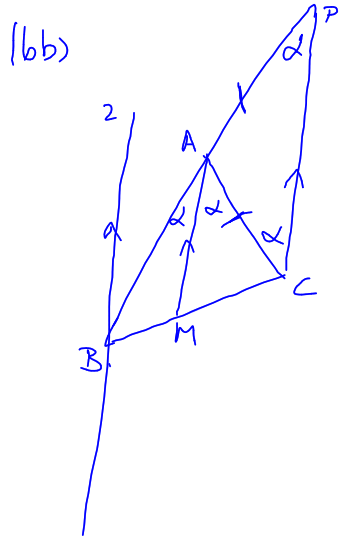
$$\therefore \frac{AD}{AB} = \frac{AE}{AC}$$

$\angle A$  is common

$\therefore \triangle ADE \parallel \triangle ABC$  (SAS, ratio  $x:y$ )

$$\therefore \frac{DE}{BC} = \frac{x}{x+y} \quad (\text{ratio sides in } \parallel \Delta\text{'s})$$

$$\frac{AF}{AG} = \frac{DE}{BC}$$



$$BM:MC = BA:AC$$

construct  $BZ \parallel MA \parallel PC$

$$\frac{BA}{AP} = \frac{BM}{MC} \quad (\text{ratio of intercepts of } \parallel \text{ lines})$$

$$AC = AP \quad (\text{proven in a})$$

$$\therefore \frac{BA}{AC} = \frac{BM}{MC}$$