

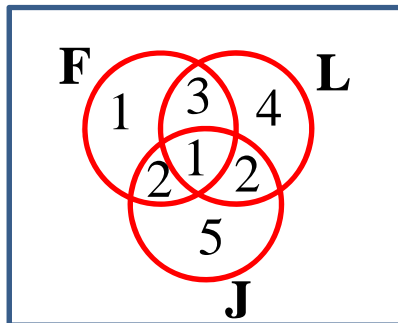
Conditional Probability

The conditional probability of an event A , given that event B has already occurred is given by;

$$P(A|B) = \frac{P(A \cap B)}{P(B)} \quad \text{or} \quad P(A|B) = \frac{|A \cap B|}{|B|}$$

*Note: if $P(A|B) = P(A)$ then A and B are independent events
or $P(A \cap B) = P(A) \times P(B)$*

e.g. (i) In a mixed language class, students study French, Latin and Japanese. The number of students who study each language are shown in the Venn diagram.



What is the probability that a student who studies Indonesian also studies French?

$$P(\text{French} | \text{Japanese}) = \underline{\underline{\frac{3}{10}}}$$

(ii) Two boxes each contain four stones that differ only in colour.

Box 1 contains four black stones

Box 2 contains two black stones and two white stones

A box is chosen at random and one stone is randomly drawn from it

a) What is the probability that the randomly drawn stone is black

$$P(\text{black}) = \frac{1}{2} + \frac{1}{2} \times \frac{2}{4} \quad \text{OR} \quad P(\text{black}) = \frac{6}{8}$$
$$= \frac{3}{4} \qquad \qquad \qquad = \frac{3}{4}$$

b) It is not known from which box the stone has been drawn.

Given that the stone drawn is black, what is the probability that it was drawn from Box 1?

$$\begin{aligned} P(\text{Box 1} | \text{black}) &= \frac{P(\text{black and Box 1})}{P(\text{black})} \\ &= \frac{\frac{1}{2} \times 1}{\frac{3}{4}} \\ &= \frac{2}{3} \end{aligned}$$

(iii) In a particular school 55% are male and 45% are female. Of the male students 13% say Monday is their favourite day, while 18% of the females say Monday is their favourite.

Find the probability that a student chosen at random is a male whose favourite day is Monday.

$$P(\text{Male}) = 0.55 \qquad P(\text{Monday}|\text{Male}) = 0.13$$

$$P(\text{Monday}|\text{Male}) = \frac{P(\text{Monday} \& \text{Male})}{P(\text{Male})}$$

$$0.13 = \frac{P(\text{Monday} \& \text{Male})}{0.55}$$

$$\begin{aligned} P(\text{Monday} \& \text{Male}) &= 0.13 \times 0.55 \\ &= \underline{0.0715} \end{aligned}$$

**Exercise 12G; 1ac, 2, 3, 5, 6ac, 7ac, 8ace, 10, 11, 13, 14, 15,
17, 18, 19, 21, 22, 25**