

10d)

~~10d)~~

$$\begin{aligned} & \frac{1}{x^2 - 4x + 3} + \frac{1}{x^2 - 5x + 6} - \frac{1}{x^2 - 3x + 2} \\ &= \frac{1}{(x-3)(x-1)} + \frac{1}{(x-3)(x-2)} - \frac{1}{(x-2)(x-1)} \\ &= \frac{(x-2) + (x-1) - (x-3)}{(x-3)(x-1)(x-2)} \\ &= \frac{x}{(x-3)(x-1)(x-2)} \end{aligned}$$

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14b)

$$\begin{aligned} & \left( 1 + \frac{45}{x-8} - \frac{26}{x-6} \right) \left( 3 - \frac{65}{x+7} + \frac{8}{x-2} \right) \\ &= \frac{(x-8)(x-6) + 45(x-6) - 26(x-8)}{(x-8)(x-6)} \times \frac{3(x+7)(x-2) - 65(x-2) + 8(x+7)}{(x+7)(x-2)} \\ &= \frac{x^2 + 5x - 14}{(x-8)(x-6)} \times \frac{3x^2 - 42x + 144}{(x+7)(x-2)} \\ &= \frac{(x+7)(x-2)}{(x-8)(x-6)} \times \frac{3(x-8)(x-6)}{(x+7)(x-2)} \\ &= \underline{\underline{3}} \end{aligned}$$

14c)

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$$\begin{aligned}
 & \left( 2 - \frac{3n}{m} + \frac{9n^2 - 2m^2}{m^2 + 2mn} \right) \div \left( \frac{1}{m} - \frac{1}{m - 2n - \frac{4n^2}{m+n}} \right) \\
 &= \left( 2 - \frac{3n}{m} + \frac{(9n^2 - 2m^2)}{m(m+2n)} \right) \div \left( \frac{1}{m} - \frac{(m+n)}{m^2 + mn - 2mn - 4n^2} \right) \\
 &= \frac{2m^2 + 4mn - 3mn - 6n^2 + 9n^2 - 2m^2}{m(m+2n)} \div \left( \frac{1}{m} - \frac{(m+n)}{m^2 - mn - 6n^2} \right) \\
 &= \frac{3n^2 + mn}{m(m+2n)} \div \left( \frac{1}{m} - \frac{(m+n)}{(m-3n)(m+2n)} \right) \\
 &= \frac{n(3n+m)}{\cancel{m(m+2n)}} \times \frac{\cancel{m(m-3n)(m+2n)}}{m^2 - mn - 6n^2 - m^2 - mn} \\
 &= \frac{n(3n+m)(m-3n)}{-6n^2 - 2mn} \\
 &= \frac{\cancel{n(3n+m)(m-3n)}}{-2\cancel{n(3n+m)}} \\
 &= \frac{3n-m}{2}
 \end{aligned}$$