

Polynomial Functions

A real polynomial $P(x)$ of degree n is an expression of the form;

$$P(x) = p_0 + p_1x + p_2x^2 + \dots + p_{n-1}x^{n-1} + p_nx^n$$

where: $p_n \neq 0$

$n \geq 0$ and is an integer

coefficients: $p_0, p_1, p_2, \dots, p_n$

index (exponent): the powers of the pronumerals.

degree (order): the highest index of the polynomial. The polynomial is called “**polynomial of degree n** ”

leading term: p_nx^n

leading coefficient: p_n

monic polynomial: leading coefficient is equal to one.

$P(x) = 0$: polynomial equation

$y = P(x)$: polynomial function

roots: solutions to the polynomial equation $P(x) = 0$

zeros: the values of x that make polynomial $P(x)$ zero. i.e. the x intercepts of the graph of the polynomial.

e.g. (i) Which of the following are polynomials?

a) $5x^3 - 7x^{\frac{1}{2}} - 2$ **NO**, can't have fraction as a power

b) $\frac{4}{x^2 + 3}$ **NO**, can't have negative as a power $4(x^2 + 3)^{-1}$

c) $\frac{x^2 + 3}{4}$ **YES**, $\frac{1}{4}x^2 + \frac{3}{4}$

d) 7 **YES**, $7x^0$

**Exercise 10A; 1, 2acehi, 3bdf,
5bd, 6b, 7, 9d, 11, 13**

(ii) Determine whether $P(x) = x^3(8x+1) + 7x - 11 - (2x^2 + 1)(4x^2 - 3)$ is monic and state its degree.

$$P(x) = 8x^4 + x^3 + 7x - 11 - 8x^4 + 6x^2 - 4x^2 + 3$$

$$= x^3 + 2x^2 + 7x - 8$$

\therefore monic, degree = 3