

Indefinite Integral

$$(1) \int x^n dx = \frac{x^{n+1}}{n+1} + c$$

$$(2) \int (ax+b)^n dx = \frac{(ax+b)^{n+1}}{a(n+1)} + c \quad (\text{must be a linear function})$$

$$\text{e.g. } (i) \int (2-5x)^3 dx = \frac{1}{4(-5)} (2-5x)^4 + c$$

$$= -\frac{1}{20} (2-5x)^4 + c$$

$$\begin{aligned}
 (ii) \int \frac{dx}{(3x+1)^2} &= \int (3x+1)^{-2} dx \\
 &= -\frac{1}{3}(3x+1)^{-1} + c \\
 &= \frac{-1}{3(3x+1)} + c
 \end{aligned}$$

$$\begin{aligned}
 (iii) \int \sqrt{2x+1} dx &= \int (2x+1)^{\frac{1}{2}} dx \\
 &= \frac{2}{3(2)} (2x+1)^{\frac{3}{2}} + c \\
 &= \frac{1}{3} (2x+1)^{\frac{3}{2}} + c \\
 &= \frac{1}{3} (2x+1) \sqrt{2x+1} + c
 \end{aligned}$$

**Exercise 5E; 2be, 7c,
8ejl, 11cj, 13ah, 14ac,
16a, 19bei, 20**